

$$\left\{
\begin{aligned}
\sigma_{pp} &= A + B \cdot \ln s + C \cdot \ln^2 s + Y_1^{pp}s^{-\eta_1} - Y_2^{pp}s^{-\eta_2}, \\
\sigma_{\bar{p}p} &= A + B \cdot \ln s + C \cdot \ln^2 s + Y_1^{pp}s^{-\eta_1} + Y_2^{pp}s^{-\eta_2}, \\
\sigma_{\pi^+p} &= \lambda_{\pi p}(A + B \cdot \ln s + C \cdot \ln^2 s) + Y_1^{\pi p}s^{-\eta_1} - Y_2^{\pi p}s^{-\eta_2}, \\
\sigma_{\pi^-p} &= \lambda_{\pi p}(A + B \cdot \ln s + C \cdot \ln^2 s) + Y_1^{\pi p}s^{-\eta_1} + Y_2^{\pi p}s^{-\eta_2}, \\
\sigma_{K^+p} &= \lambda_{K p}(A + B \cdot \ln s + C \cdot \ln^2 s) + Y_1^{K p}s^{-\eta_1} - Y_2^{K p}s^{-\eta_2}, \\
\sigma_{K^-p} &= \lambda_{K p}(A + B \cdot \ln s + C \cdot \ln^2 s) + Y_1^{K p}s^{-\eta_1} + Y_2^{K p}s^{-\eta_2}, \\
\sigma_{\gamma p} &= \lambda_{\gamma p}(A + B \cdot \ln s + C \cdot \ln^2 s) + Y_1^{\gamma p}s^{-\eta_1}, \\
\sigma_{\gamma\gamma} &= \lambda_{\gamma\gamma}(A + B \cdot \ln s + C \cdot \ln^2 s) + Y_1^{\gamma\gamma}s^{-\eta_1}, \\
\sigma_{\Sigma^-p} &= \lambda_{\Sigma p}(A + B \cdot \ln s + C \cdot \ln^2 s) + Y_1^{\Sigma p}s^{-\eta_1} - Y_2^{\Sigma p}s^{-\eta_2}. \quad \blacksquare
\end{aligned}
\right.$$
  

$$\left\{
\begin{aligned}
\rho_{pp}\sigma_{pp} &= \pi \cdot \left( \frac{B}{2} + C \cdot \ln s \right) - \frac{Y_1^{pp}s^{-\eta_1}}{\tan \left[ \frac{1-\eta_1}{2}\pi \right]} - \frac{Y_2^{pp}s^{-\eta_2}}{\cot \left[ \frac{1-\eta_2}{2}\pi \right]}, \\
\rho_{\bar{p}p}\sigma_{\bar{p}p} &= \pi \cdot \left( \frac{B}{2} + C \cdot \ln s \right) - \frac{Y_1^{pp}s^{-\eta_1}}{\tan \left[ \frac{1-\eta_1}{2}\pi \right]} + \frac{Y_2^{pp}s^{-\eta_2}}{\cot \left[ \frac{1-\eta_2}{2}\pi \right]}, \\
\rho_{\pi^+p}\sigma_{\pi^+p} &= \lambda_{\pi p} \cdot \pi \cdot \left( \frac{B}{2} + C \cdot \ln s \right) - \frac{Y_1^{\pi p}s^{-\eta_1}}{\tan \left[ \frac{1-\eta_1}{2}\pi \right]} - \frac{Y_2^{\pi p}s^{-\eta_2}}{\cot \left[ \frac{1-\eta_2}{2}\pi \right]}, \\
\rho_{\pi^-p}\sigma_{\pi^-p} &= \lambda_{\pi p} \cdot \pi \cdot \left( \frac{B}{2} + C \cdot \ln s \right) - \frac{Y_1^{\pi p}s^{-\eta_1}}{\tan \left[ \frac{1-\eta_1}{2}\pi \right]} + \frac{Y_2^{\pi p}s^{-\eta_2}}{\cot \left[ \frac{1-\eta_2}{2}\pi \right]}, \\
\rho_{K^+p}\sigma_{K^+p} &= \lambda_{K p} \cdot \pi \cdot \left( \frac{B}{2} + C \cdot \ln s \right) - \frac{Y_1^{K p}s^{-\eta_1}}{\tan \left[ \frac{1-\eta_1}{2}\pi \right]} - \frac{Y_2^{K p}s^{-\eta_2}}{\cot \left[ \frac{1-\eta_2}{2}\pi \right]}, \\
\rho_{K^-p}\sigma_{K^-p} &= \lambda_{K p} \cdot \pi \cdot \left( \frac{B}{2} + C \cdot \ln s \right) - \frac{Y_1^{K p}s^{-\eta_1}}{\tan \left[ \frac{1-\eta_1}{2}\pi \right]} + \frac{Y_2^{K p}s^{-\eta_2}}{\cot \left[ \frac{1-\eta_2}{2}\pi \right]},
\end{aligned}
\right.$$

Variable  $s$  is in the units [ $GeV^2$ ]. The additional scale  $s_1 = 1$  [ $GeV^2$ ] in terms with  $(s/s_1)^{-\eta_{1,2}}$  is omitted for brevity.

Adjustable parameters naming. In total 20 parameters used:

$$\eta_1, \eta_2, \lambda_{\pi p}, \lambda_{K p}, \lambda_{\Sigma p}, \lambda_{\gamma p}, \lambda_{\gamma\gamma} \quad - \text{ dimensionless}$$

$$A, B, C, Y_{1,2}^{pp}, Y_{1,2}^{\pi p}, Y_{1,2}^{K p}, Y_{1,2}^{\Sigma p}, Y_1^{\gamma p}, Y_1^{\gamma\gamma} \quad - \text{ [mb]}$$

Scan-fits summary. 2000 database. Without cosmic data points.

| $E_{\text{cm}}^{\min}$ [GeV]          | 3    | 4    | 5    | 6    | 7     | 8    | 9    | 10   |
|---------------------------------------|------|------|------|------|-------|------|------|------|
| $N_{dof}$ : $\rho$ excluded           | 706  | 561  | 487  | 414  | 349   | 311  | 265  | 210  |
| $N_{dof}$ : $\rho$ included           | 884  | 722  | 628  | 549  | 478   | 433  | 377  | 309  |
| $\chi^2/\text{dof}$ : $\rho$ excluded | 1.30 | 0.96 | 0.82 | 0.80 | 0.85  | 0.85 | 0.85 | 0.82 |
| $\chi^2/\text{dof}$ : $\rho$ included | 1.61 | 1.10 | 0.97 | 0.97 | 0.998 | 0.95 | 0.93 | 0.93 |

Details of the fit to the data in the whole domain of applicability

|                                     |         |     | $\chi^2/\text{dof}$      | =               | 0.97           |
|-------------------------------------|---------|-----|--------------------------|-----------------|----------------|
|                                     |         |     | CL[%]                    | =               | 69.72          |
|                                     |         |     | Name of value            | Numerical value | Error value    |
| Breakdown of the CS data sample     |         |     | $\eta_1$                 | 0.20020869      | 0.010536634    |
| $pp$ :                              | 5.00963 | 112 | $\eta_2$                 | 0.54334494      | 0.0064091006   |
| $\bar{p}p$ :                        | 5.1569  | 59  | $\lambda_{\pi p}$        | 0.68816667      | 0.0062681718   |
| $\pi^+ p$ :                         | 5.21275 | 50  | $\lambda_{K p}$          | 0.65072174      | 0.010242795    |
| $\pi^- p$ :                         | 5.02954 | 106 | $\lambda_{\Sigma p}$     | 1.0644665       | 0.058302433    |
| $K^+ p$ :                           | 5.12707 | 40  | $\lambda_{\gamma p}$     | 0.0035982407    | 0.000059308528 |
| $K^- p$ :                           | 5.10875 | 63  | $\lambda_{\gamma\gamma}$ | 9.434353E-06    | 5.4339892E-07  |
| $\Sigma^- p$ :                      | 6.12189 | 9   | $B$                      | 7.5860589       | 0.83911335     |
| $\gamma p$ :                        | 5.01008 | 38  | $A$                      | -38.50015       | 8.5802622      |
| $\gamma\gamma$ :                    | 5.      | 30  | $C$                      | -0.02800196     | 0.025777808    |
| Breakdown of the $\rho$ data sample |         |     | $Y_{pp1}$                | 113.76647       | 8.0642168      |
| $pp$ :                              | 5.30542 | 74  | $Y_{pp2}$                | 33.168757       | 0.9704665      |
| $\bar{p}p$ :                        | 11.5382 | 11  | $Y_{\pi p1}$             | 66.769441       | 6.1105925      |
| $\pi^+ p$ :                         | 8.98072 | 8   | $Y_{\pi p2}$             | 5.7639493       | 0.16248065     |
| $\pi^- p$ :                         | 7.56285 | 30  | $Y_{K p1}$               | 55.18892        | 6.1761696      |
| $K^+ p$ :                           | 5.21771 | 10  | $Y_{K p2}$               | 13.365214       | 0.38183928     |
| $K^- p$ :                           | 5.23565 | 8   | $Y_{\gamma p1}$          | 0.32421008      | 0.033242904    |
|                                     |         |     | $Y_{\gamma\gamma1}$      | 0.00089545109   | 0.000086567891 |
|                                     |         |     | $Y_{\Sigma p1}$          | 92.433612       | 11.013198      |
|                                     |         |     | $Y_{\Sigma p2}$          | 8.1833441       | 21.692103      |

#### Model quality indicators:

|             | $A^M$ | $C_1^M$ | $C_2^M$ | $U^M$ | $R_1^M$ | $R_2^M$ | $S_1^M$ | $S_2^M$ |
|-------------|-------|---------|---------|-------|---------|---------|---------|---------|
| RR(PL2)(20) | 1.595 | 69.72   | 82.05   | 17.05 | 30.86   | 0.616   | 0.013   | 1.295   |

#### Repository:

computer - NPT1

directory - d:\MathemD\Kolja\Evela\Gauron\RR(PL2)(20)

|                     | CS data    |            |           |           |         |         |              |            |                |
|---------------------|------------|------------|-----------|-----------|---------|---------|--------------|------------|----------------|
| Reaction            | $p\bar{p}$ | $\bar{p}p$ | $\pi^+ p$ | $\pi^- p$ | $K^+ p$ | $K^- p$ | $\Sigma^- p$ | $\gamma p$ | $\gamma\gamma$ |
| $\chi^2/\text{NoP}$ | 0.87       | 0.98       | 0.95      | 0.82      | 0.74    | 0.64    | 0.41         | 0.72       | 0.53           |

|                     | $\rho$ data |            |           |           |         |         |
|---------------------|-------------|------------|-----------|-----------|---------|---------|
| Reaction            | $p\bar{p}$  | $\bar{p}p$ | $\pi^+ p$ | $\pi^- p$ | $K^+ p$ | $K^- p$ |
| $\chi^2/\text{NoP}$ | 1.56        | 0.47       | 1.83      | 1.47      | 1.33    | 1.2     |

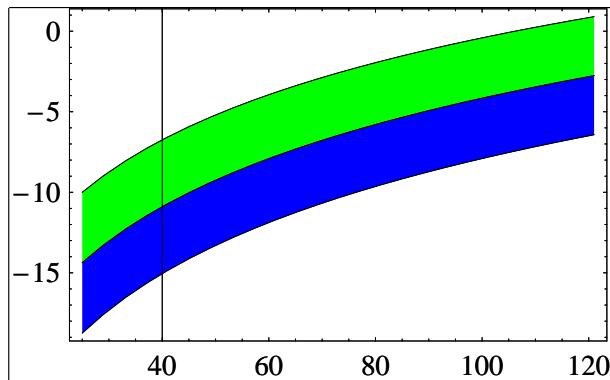


Figure 32: Pomeron contribution for  $p\bar{p}$  [mb] (Axis  $X - s$  [GeV $^2$ ])

## Appendix

### RR(PL2)(20) (N<sup>o</sup>34)

### Correlation matrix

|                           | $\eta_1$ | $\eta_2$ | $\lambda_{\pi p}$ | $\lambda_{K p}$ | $\lambda_{\Sigma p}$ | $\lambda_{\gamma p}$ | $\lambda_{\gamma \gamma}$ | $B$   | $C$   | $Y_{pp1}$ | $Y_{pp2}$ | $Y_{\pi p1}$ | $Y_{\pi p2}$ | $Y_{K p1}$ | $Y_{K p2}$ | $Y_{\Sigma p1}$ | $Y_{\Sigma p2}$ | $Y_{\gamma p1}$ | $Y_{\gamma \gamma 1}$ |       |
|---------------------------|----------|----------|-------------------|-----------------|----------------------|----------------------|---------------------------|-------|-------|-----------|-----------|--------------|--------------|------------|------------|-----------------|-----------------|-----------------|-----------------------|-------|
| $\eta_1$                  | 100      | 31.2     | -93               | -97.1           | -14                  | -75.2                | -14.4                     | -86.9 | 94.6  | 70.1      | -92       | 33.2         | -93.4        | 26.8       | -94.3      | 27.7            | -93.9           | -91.2           | -88.6                 | -9.05 |
| $\eta_2$                  | 31.2     | 100      | -12.1             | -22.3           | -3.87                | -14.9                | -3.02                     | -24.2 | 26.7  | 19.4      | -24.1     | 97.5         | -24.9        | 88.5       | -25.5      | 94.6            | -25.2           | -24.5           | -23.3                 | -1.84 |
| $\lambda_{\pi p}$         | -93      | -12.1    | 100               | 94.8            | 13.1                 | 74.6                 | 14.1                      | 83.3  | -90.2 | -67.2     | 88.9      | -12.7        | 90.1         | -8.91      | 90.6       | -9.38           | 90.3            | 87.8            | 85.4                  | 9.26  |
| $\lambda_{K p}$           | -97.1    | -22.3    | 94.8              | 100             | 13.7                 | 75.4                 | 14.4                      | 84.7  | -92.4 | -67.8     | 90.3      | -23.5        | 91.6         | -18.7      | 92.4       | -18.6           | 92              | 89.4            | 87                    | 9.16  |
| $\lambda_{\Sigma p}$      | -14      | -3.87    | 13.1              | 13.7            | 100                  | 10.5                 | 2.12                      | 10.7  | -12.3 | -8.02     | 11.7      | -4.16        | 12           | -3.48      | 12.2       | -3.45           | 12.1            | 11.7            | -18.1                 | -85.2 |
| $\lambda_{\gamma p}$      | -75.2    | -14.9    | 74.6              | 10.5            | 100                  | 11.2                 | 66.8                      | -72.4 | -54   | 71.1      | -15.7     | 72           | -12.2        | 72.5       | -12.5      | 73              | 70.3            | 68.3            | 7.27                  |       |
| $\lambda_{\gamma \gamma}$ | -14.4    | -3.02    | 14.1              | 14.4            | 2.12                 | 11.2                 | 100                       | 12.3  | -13.5 | -9.76     | 13.1      | -3.22        | 13.3         | -2.57      | 13.5       | -2.58           | 13.4            | 10.6            | 12.7                  | 1.3   |
| $B$                       | -86.9    | -24.2    | 83.3              | 84.7            | 10.7                 | 66.8                 | 12.3                      | 100   | -98.2 | -95.9     | 99.1      | -25.6        | 98.6         | -18.7      | 98.2       | -20.7           | 98.4            | 96.1            | 92.4                  | 9     |
| $A$                       | 94.6     | 26.7     | -90.2             | -92.4           | -12.3                | -72.4                | -13.5                     | -98.2 | 100   | 88.9      | -99.7     | 28.2         | -99.9        | 21.5       | -100       | 23              | -99.9           | -97.4           | -94                   | -9.4  |
| $C$                       | 70.1     | 19.4     | -67.2             | -67.8           | -8.02                | -54                  | -9.76                     | -95.9 | 88.9  | 100       | -91.4     | 20.7         | -89.9        | 14.1       | -88.9      | 16.3            | -89.4           | -87.5           | -83.6                 | -7.63 |
| $Y_{pp1}$                 | -92      | -24.1    | 88.9              | 90.3            | 11.7                 | 71.1                 | 13.1                      | 99.1  | -99.7 | -91.4     | 100       | -25.4        | 99.9         | -18.9      | 99.8       | -20.6           | 99.9            | 97.4            | 93.9                  | 9.41  |
| $Y_{pp2}$                 | 33.2     | 97.5     | -12.7             | -23.5           | -4.16                | -15.7                | -3.22                     | -25.6 | 28.2  | 20.7      | -25.4     | 100          | -26.3        | 86.4       | -26.9      | 92.2            | -26.7           | -25.9           | -24.6                 | -1.85 |
| $Y_{\pi p1}$              | -93.4    | -24.9    | 90.1              | 91.6            | 12                   | 72                   | 13.3                      | 98.6  | -99.9 | -89.9     | 99.9      | -26.3        | 100          | -19.8      | 100        | -21.4           | 100             | 97.5            | 94.1                  | 9.45  |
| $Y_{\pi p2}$              | 26.8     | 88.5     | -8.91             | -18.7           | -3.48                | -12.2                | -2.57                     | -18.7 | 21.5  | 14.1      | -18.9     | 86.4         | -19.8        | 100        | -20.4      | 83.7            | -20.1           | -19.5           | -18.5                 | -1.38 |
| $Y_{K p1}$                | -94.3    | -25.5    | 90.6              | 92.4            | 12.2                 | 72.5                 | 13.5                      | 98.2  | -100  | -88.9     | 99.8      | -26.9        | 100          | -20.4      | 100        | -21.9           | 100             | 97.5            | 94.1                  | 9.46  |
| $Y_{K p2}$                | 27.7     | 94.6     | -9.38             | -18.6           | -3.45                | -12.5                | -2.58                     | -20.7 | 23    | 16.3      | -20.6     | 92.2         | -21.4        | 83.7       | -21.9      | 100             | -21.7           | -21             | -19.9                 | -1.51 |
| $Y_{\Sigma p1}$           | -93.9    | -25.2    | 90.3              | 92              | 12.1                 | 73                   | 13.4                      | 98.4  | -99.9 | -89.4     | 99.9      | -26.7        | 100          | -20.1      | 100        | -21.7           | 100             | 97.5            | 94.1                  | 9.46  |
| $Y_{\Sigma p2}$           | -91.2    | -24.5    | 87.8              | 89.4            | 11.7                 | 70.3                 | 10.6                      | 96.1  | -97.4 | -87.5     | 97.4      | -25.9        | 97.5         | -19.5      | 97.5       | -21             | 97.5            | 100             | 91.7                  | 9.21  |
| $Y_{\gamma p1}$           | -88.6    | -23.3    | 85.4              | 87              | -18.1                | 68.3                 | 12.7                      | 92.4  | -94   | -83.6     | 93.9      | -24.6        | 94.1         | -18.5      | 94.1       | -19.9           | 91.7            | 100             | 42.6                  | 42.6  |
| $Y_{\gamma \gamma 1}$     | -9.05    | -1.84    | 9.26              | 9.16            | -85.2                | 7.27                 | 1.3                       | 9     | -9.4  | -7.63     | 9.41      | -1.85        | 9.45         | -1.38      | 9.46       | -1.51           | 9.46            | 9.21            | 42.6                  | 100   |

## Appendix RR(PL2)(20) (Nº34) Parameters evolution

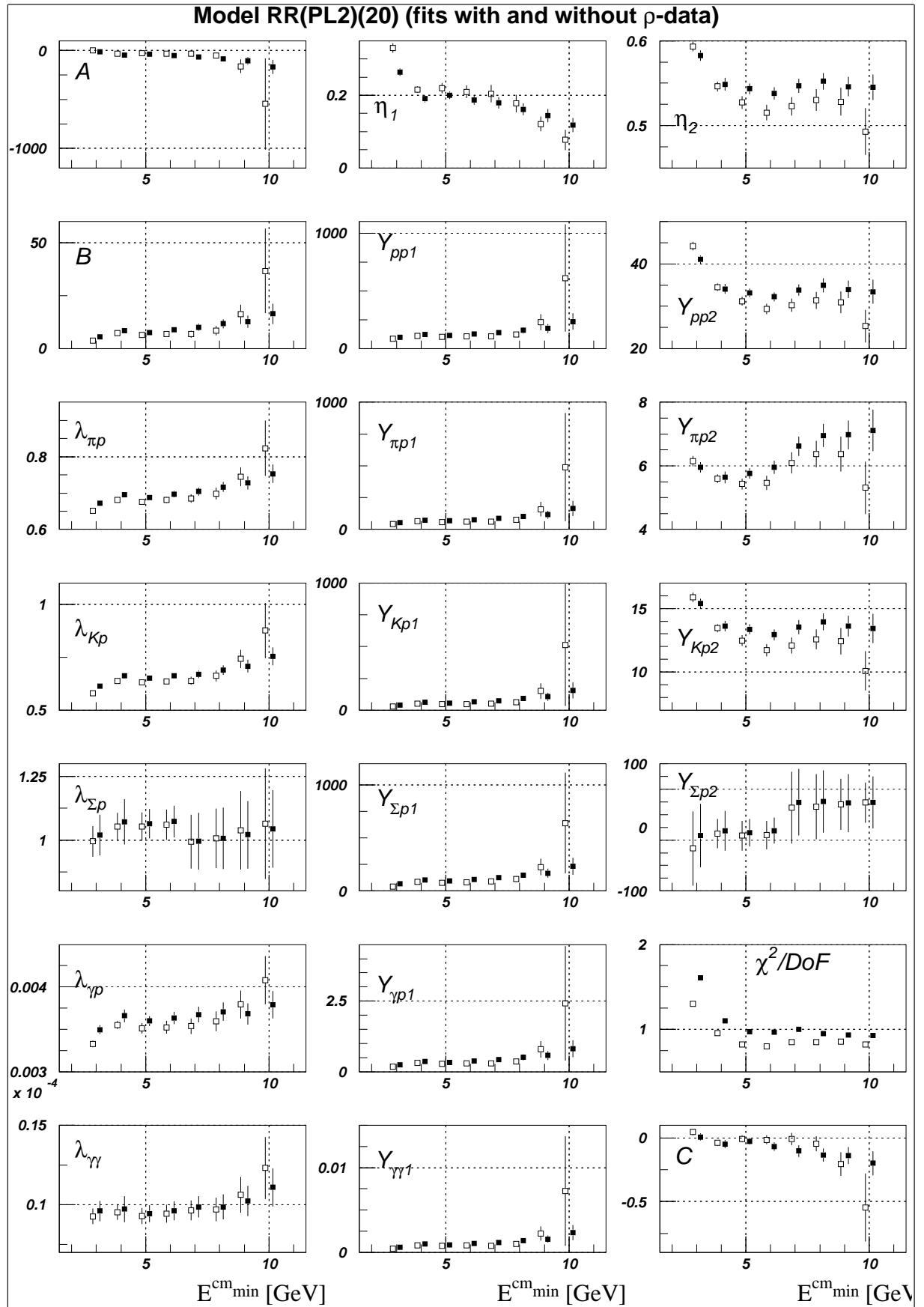


Figure 33: Bold (empty) symbol marks fits with (without)  $\rho$  data and are shifted to the right (left) in energy slightly for the clearness

